## ECON 7920 Econometrics II Philip Shaw Problem Set 4 Due Date: April 4, 2023

Chapter 13 Problems: 13.1, 13.2, 13.3

## Problem 1

Using the data set apple.csv, create a variable ecobuy = I(ecolbs > 0). Using as the explanatory variables regprc, ecoprc, and age conduct the following analysis.<sup>1</sup>

a. Under the assumption that the structural error term is independent of all x-variables and has a standard normal distribution derive the log-likelihood function.

b. Using the log-likelihood function from above, modify the qfunction.R script file to estimate the parameters of interest via M-estimation.

c. Compute the t statistics under the zero null for each of the x-variables on interest. Do you reject the zero null for all variables?

d. Now using the probit command in R, compare your results to the ones under probit estimation. Do you conclusions change?<sup>2</sup>

e. Now compute the likelihood ratio test under the null hypothesis that *ecoprc* and *age* are jointly insignificant in determining P(ecobuy = 1|x). Do you reject the null hypothesis?<sup>3</sup>

 $<sup>^1\</sup>mathrm{For}$  this problem you will need the script files q function.R, qderivfun.R, and qderivfun2.R.

<sup>&</sup>lt;sup>2</sup>probitout =  $glm(y \sim x, family=binomial(link="probit"))$ 

<sup>&</sup>lt;sup>3</sup>Recall the command in R for the Chi-squared distribution function is dchisq(LR,Q).